# HYBRID SUBJECTIVE EVALUATION OF RULE EXTRACTION ALGORITHM USING WEIGHTED SUBSETHOOD-BASED (WSBA) OF FINANCIAL PERFORMANCE

## Mahmod Othman<sup>1</sup>, Ku Ruhana Ku-Mahamud<sup>2</sup>, Shezrin Hawani, Amir Hamzah<sup>3</sup>, Shaiful Annuar Khalid<sup>4</sup>, and Fader Abdullah<sup>5</sup>

<sup>1</sup>Universiti Teknologi MARA Perlis. Arau, Perlis, mahmod135085@perlis.uitm.edu.my <sup>2</sup>Universiti Utara Malaysia, Sintok, Kedah, ruhana@uum.edu.my <sup>3</sup>Universiti Teknologi MARA Perlis. Arau, Perlis, yin\_sherini@yahoo.com <sup>4</sup>Universiti Teknologi MARA Perlis. Arau, Perlis, shaiful@perlis.uitm.edu.my <sup>5</sup>Universiti Teknologi MARA Perlis. Arau, Perlis, fader@perlis.uitm.edu.my

**ABSTRACT**. Fuzzy rules are important elements that being highlighted in any fuzzy expert system. This research proposes the framework of subjective performance evaluation using fuzzy technique for ranking the performance of the financial performance of a company under a multicriteria environment. There are a lot of techniques used such as fuzzy similarity function, fuzzy synthetic decision and satisfaction function have been adopted. The framework is based on fuzzy multi-criteria decisionmaking that consists of fuzzy rules. The use of fuzzy rules, which were extracted directly from input data through Weighted Subsethood-based (WSBA) Rule Generation Algorithm. WSBA rule generation use the subsethood values to generate the weights which finally produced the fuzzy general rules. The rules generated through the data provided knowledge in developed fuzzy rule The fuzzy rules embedded in the framework of subjective evaluation method showed advantages in generalizing the evaluation of the performance achievement, where the evaluation process can be conducted consistently in producing good evaluation results with the use of the membership set score. The results from the numerical examples are comparable to other fuzzy evaluation methods, even with the use of small rule size.

Keywords: fuzzy technique; weighted subsethood based; rule generations

#### INTRODUCTION

Decision making environment involves a lot of important information which help to generate fuzzy rule generation. With more data collection, the increasing on knowledge involve that will help in order to generate the fuzzy rules. To be more realistic, in evaluation problems there involve many subjectivity, vagueness and imprecise information. Therefore, the use of fuzzy set theory which focuses on the rule generation will help to improve the result on evaluation. Most of the rule generation derive from the data collection as the input that have been discussed in Hong(1996), Yager (1991) and Wang (1992). They stated on how the fuzzy rules was generated from the membership functions which adapted from the input data. This method helped to reduce the time and effort other than by developing the fuzzy expert system.

In order to generates rules, there involves all the possible combinations of the fuzzy partitions of the input variables. Basically, if there are only two input variables and three

fuzzy partitions for each variable, 9 rules will be generated. The outcome result will be produce by working on with the rule generated together with the defuzzification of the output.

Most subjective evaluation represents the human knowledge. The model can be represented in form of IF-THEN rules. A simple fuzzy IF-THEN rules is written in form of IF x is A THEN y is B where A and B are fuzzy sets. The fuzzy IF-THEN rules involve the antecedents and consequences which explain the fuzzy condition. A more complex fuzzy application system consisted of many fuzzy IF-THEN rules. According to Mendel (2001), there are six different types of fuzzy rules which are Incomplete rules, Mixed Rules, Fuzzy Statement Rules, Comparative Rules, Unless Rules and Quantifiers Rules. There are two type of linguistic fuzzy model that broadly used are Mamdani –type FRBS and Takagi-Sugeno-Kang (TSK).

According to Rasmani (2006), the WSBA was used for rules generation is because the subsethood values is used as weights over the significance for different conditions available which results in the conclusion. He modified Subsethood- Based techniques which ease the rule- learning process. The weight was obtained from the subsethood values then generated the rules for each possible conclusion.

In classical theories, the statement used to define a certain set usually involves two mantic values. That is, a particular statement must have a clear truth value of either true or false, yes or no, but not both of them. The truth value is usually represented by numerical value zero or one. On the contrary, in fuzzy set theory approach, a statement can have values in the range of [0, 1]. In this paper the proposed framework subjective evaluation method evaluate the financial analysis can help all the investors to make analysis on the company's financial performance. Using the financial performance data, we will rank in order to prioritize the company in an industry. This approach gives more space to measure subjective criteria to improve the expressions and assessments under the fuzzy environment.

The paper is organized as follows: In section 2, the fuzzy rule generation method is described and section 3 presents algorithm of the proposed subjective evaluation method. Section 4 will presents the numerical results and concluding remarks are given in section 5.

#### CASE STUDY

This study is using the secondary data that adopted from Tavakkoli et al (2010). There are 19 companies involve in this financial performance evaluation. The criteria that have been chosen are Return on Investment (ROI), Current Ratio, Loan Profitability and Rapid Ratio. At the final stage, the ranking will be compared and proved that the new rule extraction method can be used in this research.

The industries that have been chosen are in Iran. In financial term, the Factor Analysis method used to choose the right criteria in order to make the evaluation. The levels of financial performance will priorities the company in the industries.

### THE PROPOSED HYBRID SUBJECTIVE EVALUATION METHOD

The proposed method is based on the work done by Rasmani (2006) and Othman et al. (2008) on the use of similarity function and synthetic decision-making. However, this method focuses on extracting rules and membership set score from data which is different from the works of Rasmani (2006) and Othman et al. (2008). The proposed method uses the fuzzy rules which are determined by the rule generation. The rule generation is the enhancement of the Rasmani (2006) fuzzy rule generation method which based on Weight Subsethood algorithm is embedded in the subjective evaluation method. The use of fuzzy

rules, which are extracted from the data input in making evaluation, contributes a better decision in selecting the best choice and reduce the expert view which will takes some time.

The proposed method consisted of two phase. The initial phase consisted of three steps of fuzzy rules generation method. The second phase involved integrating the fuzzy rules into nine steps of the proposed subjective evaluation method. The first step of the initial phase is to classify the financial data into subgroups base on the criteria that have been chosen are Return on Investment (ROI), Current Ratio, Loan Profitability and Rapid Ratio. Next step is to calculate fuzzy subsethood values to obtain for every variable in each subgroup.

The Fuzzy Subsethood values can be defined as follow. Let A and B be two fuzzy set defined on the universe U. The fuzzy subsethood value of A with regard to B, S(B,A) represents the degree to which A is subsethood of B.

$$\Sigma(\mathbf{B},\mathbf{A}) = \frac{M(B \wedge A)}{M(B)} = \frac{\sum_{x \in U} \nabla(\mu_B(x), \mu_A(x))}{\sum_{x \in U} \mu_B(x)}$$

where  $S(B, A) \in [0, 1]$  and  $\nabla$  is the t-norm operator.

The related weight for the linguistic terms  $A_i$  with regard to classification X is calculated using equation below.

$$\omega(\Xi, A_i) = \frac{S(X, A_i)}{\max_{i=1, 2, \dots, l} S(X, A_j)}$$

Let  $w(X,A_i) \in [0,1]$  and i = 1,2...,l

The linguistic terms are attached with the weight generated which associates with the attributes. The equation below is used to calculated weight conjunction of linguistic terms

$$T(A) = \left(\frac{w_1}{w}(A_1)\nabla...\nabla\frac{w_m}{w}(A_m)\right)$$

where A is the conditional attribute T(A) is the compound weight and  $\nabla$  is the *t*-norm,  $A_i$ ,  $i_= 1, 2, ..., m$ , are the linguistic terms of variable A which are conjunctively combined and w is the largest amongst the m associated weights.

For the compound weight T(B) of the weighted disjunction of linguistic terms associated with variables *B* is calculated as in equation below.

$$T(B) = \left(\frac{w_1}{w}(B_1)\Delta...\Delta\frac{w_m}{w}(B_m)\right)$$

Where  $\Delta$  is the *t*- conorm and  $B_i$ , i=1,2,..., *n* are the linguistic terms B, which are disjunctively combined.

There are five steps in the proposed method to evaluate the financial performance. The first step is to calculate the normalized synthetic score value. The next three steps in this

proposed method deal with the evaluation of the attribute rule value and the appraisal product value followed by the calculation of the satisfaction value. Lastly, the ranking of the students' performance based on the satisfaction value were done, where the biggest value would indicate the best student quality performance. Results of the transformation of the Normalized Synthetic Score Value for quality attribute  $F_i$  of each cases are shown in Table 1.

Case	Factor								
	$F_1$	F2	F3	F.					
1	0.079	0.080	0.062	0.066					
2	0.083	0.082	0.078	0.094					
3	0.083	0.088	0.088	0.067					
4	0.082	0.098	0.056	0.088					
5	0.088	0.076	0.072	0.086					
6	0.100	0.076	0.042	0.061					
7	0.100	0.074	0.054	0.089					
8	0.055	0.092	0.04	0.080					
9	0.069	0.068	0.04	0.089					
10	0.037	0.082	0.032	0.092					
11	0.062	0.070	0.032	0.068					
12	0.083	0.06	0.044	0.080					
13	0.097	0.056	0.044	0.094					
14	0.056	0.078	0.052	0.027					
15	0.010	0.048	0.034	0.080					
16	0.059	0.044	0.032	0.065					
17	0.029	0.076	0.020	0.099					
18	0.052	0.028	0.100	0.055					
19	0.054	0.034	0.100	0.000					

**Table 1: Normalized Synthetic Score Value** 

The decision criteria  $DC_i$  (for i = 1, 2, 3, ..., m) is the intersection or combination of factor rules which is in the form of antecedent of the rule. The precedent of the rule indicates the conclusion in terms of linguistic variable  $A_k$  (k = 1, 2, ..., K). The linguistic variables are described by satisfactory, very satisfactory, very satisfactory, perfect and unsatisfactory respectively. The appraisal set is defined as  $A = \{A_k\}, k = 1, 2, ..., 5$ , where  $v \in V$ , the unit appraisal space  $V = \{v_l\} = \{0, 0.1, 0.2, ..., 1\}$  and l = 1, 2, ..., 11. The rule value in Table 1 is obtained by processing the normalized synthetic score value according to the multi-criteria decision of Table 2.

Decision	Factor Rule	Description	Grade	Appraisal
Criteria				Set
<i>C</i> <sub>1</sub>	$F_1 \cap F_2$	Unsatisfactory	Poor	1-v
C2	$F_1 \cap F_2 \cap F_2$	Satisfactory	Average	v
С;	$F_1 \cap F_2 \cap F_4$	Very <u>Very</u> Satisfactory	Good	v²

Table 2. Multicriteria Rules Combination	Table 2	2. Mul	lticriteria	Rules	Combination
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The combination of multi-criteria rule from Table 2 can be written as in equation below also known as fuzzy rule and the approximate reasoning is used to calculate the factor rule value.

If 
$$(C_i = \bigcap_{j=1}^4 \cup F_j)$$
 THEN  $A_k$ 

where,  $C_i$  is the decision criteria,  $F_j$  represents the factor rules (j = 1, 2, 3, 4),  $A_k$  is the linguistic variable and k stands for grade. The symbols  $\bigcup$ ,  $\bigcap$  stand for the union and the intersection respectively. The factor rule value in Table 3 is obtained by processing the normalized synthetic score value according to the multi-criteria decision of Table 2.

	<i>C</i> <sub>1</sub>	<i>C</i> <sub>2</sub>	<i>C</i> <sub>3</sub>
1	0.079	0.062	0.062
2	0.082	0.078	0.078
3	0.083	0.083	0.067
4	0.082	0.056	0.056
5	0.076	0.072	0.072
6	0.076	0.042	0.042
7	0.074	0.054	0.054
8	0.055	0.040	0.040
9	0.068	0.040	0.040
10	0.037	0.032	0.032
11	0.062	0.032	0.032
12	0.060	0.044	0.044
13	0.056	0.044	0.044
14	0.056	0.052	0.027
15	0.048	0.034	0.034
16	0.044	0.032	0.032
17	0.029	0.020	0.020
18	0.028	0.028	0.052
19	0.034	0.034	0.000

Table 5. Factor rule valu	Fable	3. Fa	ctor	rule	valı	le
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The appraisal product value is computed through the identification of the appraisal fuzzy value for *n* decision criteria. Each entry of appraisal fuzzy value  $D_j$  for every decision criteria is computed as follows:

$$d_j(m,l) = 1 \wedge (1 - \tilde{c}(u_m) + A_k(v_l))$$

where j = 1, 2, 3, ..., m, l = 1, 2, ..., 11 and  $\tilde{c}(u_m)$  is the factor rule value. The appraisal fuzzy value of for the decision criteria is shown in Table 4.

Case	Appraisal Set										
1	1	1	1	1	1	1	1	1	1	1	0.9210
2	1	1	1	1	1	1	1	1	1	1	0.9180
3	1	1	1	1	1	1	1	1	1	1	0.9170
4	1	1	1	1	1	1	1	1	1	1	0.9180
5	1	1	1	1	1	1	1	1	1	1	0.9240
6	1	1	1	1	1	1	1	1	1	1	0.9240
7	1	1	1	1	1	1	1	1	1	1	0.9260
8	1	1	1	1	1	1	1	1	1	1	0.9450
9	1	1	1	1	1	1	1	1	1	1	0.9320
10	1	1	1	1	1	1	1	1	1	1	0.9630
11	1	1	1	1	1	1	1	1	1	1	0.9380
12	1	1	1	1	1	1	1	1	1	1	0.9400
13	1	1	1	1	1	1	1	1	1	1	0.9440
14	1	1	1	1	1	1	1	1	1	1	0.9440
15	1	1	1	1	1	1	1	1	1	1	0.9520
16	1	1	1	1	1	1	1	1	1	1	0.9560
17	1	1	1	1	1	1	1	1	1	1	0.9710
18	1	1	1	1	1	1	1	1	1	1	0.9720
19	1	1	1	1	1	1	1	1	1	1	0.9660

## Table 4. Appraisal Fuzzy Value For Decision Criteria C<sub>1</sub>

Therefore, the appraisal product value D is calculated by multiplying all elements of the appraisal fuzzy value obtained earlier, with  $D_i$  following the formula given in equation below.

$$\mathbf{D} = \left( \prod_{j=1}^{J} d_j(m, l) \right) = \left( \widetilde{E}_1, \widetilde{E}_2, ..., \widetilde{E}_F, ..., \widetilde{E}_L \right) \in M_{L \times 1}$$

The appraisal product value for the financial performance is shown in Table 5.

**Table 5. Appraisal Product Value** 

Case	Appraisal Set										
1	0.8798	0.9480	0.9780	1	1	1	1	1	1	1	0.9210
2	0.8510	0.9320	0.9620	1	1	1	1	1	1	1	0.9180
3	0.8556	0.9430	0.9730	1	1	1	1	1	1	1	0.9170
4	0.8911	0.9540	0.9840	1	1	1	1	1	1	1	0.9180
5	0.8612	0.9380	0.9680	1	1	1	1	1	1	1	0.9240
6	0.9178	0.9680	0.9980	1	1	1	1	1	1	1	0.9240
7	0.8949	0.9560	0.9860	1	1	1	1	1	1	1	0.9260
8	0.9216	0.9700	1	1	1	1	1	1	1	1	0.9450
9	0.9216	0.9700	1	1	1	1	1	1	1	1	0.9320
10	0.9370	0.9780	1	1	1	1	1	1	1	1	0.9630
11	0.9370	0.9780	1	1	1	1	1	1	1	1	0.9380
12	0.9139	0.9660	0.9960	1	1	1	1	1	1	1	0.9400
13	0.9139	0.9660	0.9960	1	1	1	1	1	1	1	0.9440
14	0.9224	0.9830	1	1	1	1	1	1	1	1	0.9440
15	0.9332	0.9760	1	1	1	1	1	1	1	1	0.9520
16	0.9370	0.9780	1	1	1	1	1	1	1	1	0.9560
17	0.9604	0.9900	1	1	1	1	1	1	1	1	0.9710
18	0.9215	0.9580	0.9880	1	1	1	1	1	1	1	0.9720
19	0 9660	1	1	1	1	1	1	1	1	1	0 9660

Finally, the financial performance can be ranked using the satisfaction value, SV(m), as given below:

$$SV(m) = \frac{1}{\alpha_{maks}} \sum_{l=1}^{L} H_l(E_{m\alpha}) \Delta \alpha_l$$

where  $\alpha$  = degree of appraisal product value D;  $\Delta \alpha_l = \alpha_l - \alpha_{l-1}$ ;  $\alpha_0 = 0$ ;  $H_l(E_{m\alpha})$  = mid-point of  $V_l$  (l = 1, 2, 3, ..., L); and  $\alpha_{max}$  = maximum degree of appraisal product value. The calculated values of the range of appraisal product value ( $\alpha$ ), the difference of range of appraisal product value ( $\Delta \alpha_l = \alpha_l - \alpha_{l-1}$ ), and mean value of  $E_{m\alpha}$ , ( $H_l(E_{m\alpha})$ ) are tabulated in Table 6.

1	Range α	$E_{ma}$	H <sub>l</sub> (E <sub>n</sub>	$\Delta lpha_i$
1.	$0.0000 < \alpha \le 0.8798$	{0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1}	0.50	0.8798
2.	$0.8798 < \alpha \le 0.9210$	{0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1}	0.55	0.0412
3.	0.9210 < α ≤ 0.9480	{0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1}	0.50	0.0270
4.	0.9480<α ≤0.9780	{0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1}	0.55	0.0300
5.	0.9780 < α ≤ 1	{0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1}	0.60	0.0220
6.	1.0000<α ≤1	{0.5, 0.6, 0.7, 0.8, 0.9, 1}	0.65	0.0000
7.	$1.0000 < \alpha \le 1$	{0.6, 0.7, 0.8, 0.9, 1}	0.70	0.0000
8.	$1.0000 < \alpha \le 1$	{0.7, 0.8, 0.9, 1}	0.75	0.0000
9.	$1.0000 < \alpha \le 1$	{0.8, 0.9, 1}	0.80	0.0000
10.	$1.0000 < \alpha \le 1$	{0.9,1}	0.85	0.0000
11.	1.0000<α≤1	{1}	1	0.0000

Table 6. Calculated Range Of  $\alpha$ ,  $\Delta \alpha_l$ , and  $H_l(E_{n\alpha})$ 

The highest satisfaction value is considered as the best performance which implies that the lecturer are much more satisfied with the students score as discussed in Othman et al (2008).

## NUMERICAL RESULT

Comparison of results between the statistical method, Rasmani (2002) and the proposed method are exhibited in Table 10 the financial performance are ranked based on the satisfaction values. The experimental results show that the proposed method is comparable to Rasmani (2002). The model is in fact better because of the use of fuzzy rules in making a good ranking in accordance with human decision making (Ku Mahamud, 2010). The method has shown good consistency in accuracy in ranking with shorter rule properties where there are only three (3) rules with a minimum length of one (1) and the maximum length of three (3). In addition, the most important feature is that the developed rules have extracted the knowledge from the data input and hence are more understandable to humans. The experiment on data normalization in the model was seen as significant to stabilize the input data since there are extreme values in the input data. Noise or bias in the data distribution can be diminished through data normalization which is one of the objectives of the model. The use of rules is demonstrated to be reliable as it works like human thinking and meets the goals assessment. The quality of a method depends on the properties of the method and of the the functions for which the method is designed .The model had exhibited a good method fulfilled three major properties: (1) formal consistency; (2) usefulness; (3) where it had efficiency in the desired function at minimum effort, time and cost.

		Tavakkoli		Proposed			
Case	Panga	Description	Company	Panga	Description	Company	
	Range	Sample		Kange	Sample		
1	0.60-0.38	High	X18	0.5093-0.5063	High	X18	
2	0.60-0.38	High	X <sub>6</sub>	0.5093-0.5063	High	X6	
3	0.60-0.38	High	X4	0.5093-0.5063	High	$X_4$	
4	0.60-0.38	High	X14	0.5093-0.5063	High	X14	
5	0.60-0.38	High	X9	0.5093-0.5063	High	X9	
6	0.60-0.38	High	X10	0.5093-0.5063	High	$X_2$	
7	0.37-0.28	Moderate	X13	0.5062-0.5049	Moderate	X13	
8	0.37-0.28	Moderate	X19	0.5062-0.5049	Moderate	X19	
9	0.37-0.28	Moderate	X3	0.5062-0.5049	Moderate	$X_3$	
10	0.37-0.28	Moderate	X5	0.5062-0.5049	Moderate	$X_5$	
11	0.37-0.28	Moderate	X <sub>8</sub>	0.5062-0.5049	Moderate	$X_8$	
12	0.37-0.28	Moderate	X17	0.5062-0.5049	Moderate	$X_{10}$	
13	0.37-0.28	Moderate	X2	0.5039-0.5000	Low	X17	
14	0.27-0.00	Low	X11	0.5039-0.5000	Low	X11	
15	0.27-0.00	Low	X1	0.5039-0.5000	Low	$X_1$	
16	0.27-0.00	Low	X <sub>12</sub>	0.5039-0.5000	Low	X12	
17	0.27-0.00	Low	$X_7$	0.5039-0.5000	Low	$X_7$	
18	0.27-0.00	Low	X16	0.5039-0.5000	Low	X16	
19	0.27-0.00	Low	X15	0.5039-0.5000	Low	X15	
Accuracy		100	%	84.21%			

Table 7. Comparison of the Result

In this research, the determination method is adopted from Khairul Anwar Rasmani (2002) integrated with subjective evaluation method Othman *et al* (2008). The experimental result in Table 7, show that the proposed new range according to the fuzzy approach is comparable to the conventional range with accuracy is 84.21%. Therefore, the proposed method can be used as an alternative way in order to evaluate the financial performance of company. The factor rule produce from the WSBA rule generation also automatically can be used based on the comparable result produced for the range between the conventional and the proposed. There are 19 companies that have been evaluated and based on the proposed method, there are 18 company that same rank according to the previous method. The accuracy not reaches 100% because there some indicators that not being include in the proposed method.

#### CONCLUSION

This research proposed the new rule generation method based on WSBA rule generation adapted from Khairul Anwar Rasmani (2002). This paper also produces the new range which can also be used in financial performance evaluation. The result gain shows that the new range on the financial status of the company can be used as an alternative way with the new rule generation method which is more easy to understand and implement in the fuzzy evaluation approach in subjective way. This rule generation method on WSBA rule generation which employs the linguistic fuzzy model in the generation process will reflects how human make evaluation and judgments in the real world. This evaluation can reduce the problems that involve uncertainty which is very subjective. In this research, the main advantages and contribution is we proposed one new platform in order to generate rules which involves the simplicity with reducing in number of rules used and can be apply in different level of evaluation. Meanwhile, rules which are directly extracted from input data contribute the better decision with less reliable from the input data (Ku-Mahamud et can al, 2010). The model has been implemented using the C++ programming language and it was design for many type of fuzzy evaluation data. In many problems that involve uncertainty and subjectivity, this method can act as an alternative approach to solve problems with uncertainty such as the evaluation performance.

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